

effectiveness between different sets of parameters for the same system.

This article proposes an approach to designing a position and anti-vibration controller for tower cranes, based on the SMC method that integrates the following functions:

- A hierarchical structure for the sliding mode controller.
- Employing an optimization algorithm PSO for selecting SMC's parameter to reduce the system's setting time and lower the load's angle.

Because the tower crane is an under-actuated system, the hierarchical sliding controller was designed and utilized. In addition, the PSO algorithm will help to find parameter values to achieve the goal of optimizing setup time and reducing load swing angle deviation.

The rest of this paper is organized as follows: Section 2 introduces a dynamic model of a tower crane and details important components of this model; Section 3 presents the design of the SMC controller, developed for position control and vibration suppression of tower cranes. This is an important part, explaining in detail the SMC sliding control method and how to apply it to the tower crane system; Section 4 introduces the PSO optimization algorithm to adjust parameters in the controller. This section demonstrates how to apply the PSO algorithm to find optimal parameters for the SMC controller; Section 5 presents simulation results on Matlab/Simulink and provides results from the experimental model. This is the part to evaluate the performance and effectiveness of the proposed method through simulation and experimental results; Finally, Section 6 is the conclusion, summarizing the results and emphasizing the contributions and limitations of the research, while also suggesting future development directions.

2. Tower Crane system dynamic

The physical model of the tower crane illustrated in Figure 1, includes two motions which are the translation motion of the trolley on the jib and the slewing motion of the jib around the tower. The cargo mass m_c is attached to the trolley through a cable system that is responsible for lifting and lowering loads. When a force and a torque are acted on the trolley and the jib, the load will vibrate due to fictitious force during movement. In this system, considering only the translation motion and the slewing motion, ignoring the mass of the rope and the elastic deformation of the tower, assuming that the load angles are small, and the length of the cable stays unchanged, Euler-Lagrange equations are used to obtain the dynamics of the tower crane.

The kinetic energy of the tower crane is calculated as:

$$K = \frac{1}{2} m_t \dot{x}_t^2 + \frac{1}{2} m_c \dot{x}_c^2 + \frac{1}{2} J \dot{\gamma}^2 \quad (1)$$

where:

\dot{x}_t is the velocity of the trolley.

\dot{x}_c is the velocity of the load.

$\dot{\gamma}$ is the angular velocity of the jib.

The potential energy of the tower crane is determined as:

$$P = -m_c g l \cos \beta \cos \alpha \quad (2)$$

From (1) and (2), the Lagrange function is established as:

$$L = K - P = \frac{1}{2} m_t \dot{x}_t^2 + \frac{1}{2} m_c \dot{x}_c^2 + \frac{1}{2} J \dot{\gamma}^2 + m_c g l \cos \beta \cos \alpha \quad (3)$$



Figure 1. Tower crane model.

Corresponding to each state variable, the dynamic equations are established [32]:

$$\begin{cases} \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{R}} \right) - \frac{\partial L}{\partial R} = u_t \\ \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\gamma}} \right) - \frac{\partial L}{\partial \gamma} = u_r \\ \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\alpha}} \right) - \frac{\partial L}{\partial \alpha} = 0 \\ \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{\beta}} \right) - \frac{\partial L}{\partial \beta} = 0 \end{cases} \quad (4)$$

Ignoring the small complicated non-linear components, trigonometric approximations are also used to simplify the calculations (4), the dynamics model of the tower crane is obtained:

$$\begin{cases} \ddot{R} + \frac{m_c}{m_t} g \alpha = \frac{u_t}{m_t} \\ \left(1 + \frac{m_t}{J} R^2 \right) \ddot{\gamma} - \frac{m_c}{J} g R \alpha = \frac{u_r}{m_t} \\ l \ddot{\alpha} + g \alpha - \ddot{R} = 0 \\ l \ddot{\beta} + g \beta + R \ddot{\gamma} = 0 \end{cases} \quad (5)$$

The differential equations in (5) describe the variation of state variables, including the trolley position R , the rotation angle γ of the jib, and the swing angles α and β of the load. The state variables depend on the input variables, including the force u_t acts on the trolley, the torque u_r acts on the jib, and model parameters such as m_t , l , m_c , J , and g .

In practice, the movement of the trolley R and the jib γ are controlled independently by two motors with drivers allowing us to control the speed of the trolley and the jib separately, accurately, and eliminate the effect of external disturbances. Although equation (5) has four state variables, there are only two actuators, making the system an under-actuated system. We can see that the first and second equations in (5) interact with the swing angle state variable α . However, in this study, by using motor drivers with ideal current loops and speed loops, the influence of angle α on the first two equations can be eliminated. Besides, because the inner circuit which is used to drive the motors, is much faster than the outer speed circuit,

according to [33] we can simplify the first equation. and the second of (5) as follows:

$$\frac{R(s)}{U_t(s)} = \frac{F_1}{s(T_1s+1)} \quad (6)$$

Where, $U(s)$ is the Laplace transformation of the voltage signal control the trolley $u_t(t)$, $R(s)$ is the Laplace transformation of the position of the trolley $r(t)$, F_1 is a gain factor, and T_1 is the time constant of the system.

Inverse Laplace transform equation (6), we have:

$$\ddot{R} + \frac{1}{T_1} \dot{R} = \frac{F_1}{T_1} u_t \quad (7)$$

Similarly, the model that controls the rotation angle of the jib can be expressed as:

$$\dot{\gamma} + \frac{1}{T_2} \gamma = \frac{F_2}{T_2} u_r \quad (8)$$

The dynamic model of the tower crane can be rewritten as follows:

$$\ddot{R} + \frac{1}{T_1} \dot{R} = \frac{F_1}{T_1} u_t \quad (9)$$

$$\dot{\gamma} + \frac{1}{T_2} \gamma = \frac{F_2}{T_2} u_r \quad (10)$$

$$l\ddot{\alpha} + g\alpha - \ddot{R} = 0 \quad (11)$$

$$l\ddot{\beta} + g\beta + R\dot{\gamma} = 0 \quad (12)$$

It should be noted here that we will design the position and angle control by including the motor transmission system, so the input control signal has been converted to voltage. In this study, we will use equations (9)-(12) to design a controller for the tower crane in the next section.

3. Controller design and control parameter optimization

3.1. Design of the Hierarchical Sliding Mode Controller

According to the dynamics model (9)-(12), the tower crane is an under-actuated system. The purpose of this paper is to design a controller that drives the trolley and the jib to the desired position and reduces the swing angles of the cargo to zero. A hierarchical sliding mode control approach is proposed to control the under-actuated system such as the tower crane with u_t , u_r are the control inputs and R , γ , α , β are the system state. Designing of the HSMC includes two steps:

- First, a first-order sliding surface is defined to attract all state trajectories.
- Then a control scheme is built to force all system states to their reference values on the sliding surface.

Set the system state R , γ , α , β as state variables as follow:

$$\begin{aligned} x_1 &= R; x_2 = \dot{x}_1; x_3 = \gamma; x_4 = \dot{x}_3; \\ x_5 &= \alpha; x_6 = \dot{x}_5; x_7 = \beta; x_8 = \dot{x}_7 \end{aligned} \quad (13)$$

Define the regulation error vectors as follows:

$$e_1 = x_1 - x_{1d}; e_3 = x_3 - x_{3d}; e_5 = x_5; e_7 = x_7 \quad (14)$$

Substituting (13) into equations (9)-(12) and presenting them in the state-space model, one can obtain the state-space model of the tower crane as follows:

$$\begin{aligned} \dot{x}_1 &= x_2; & \dot{x}_2 &= \frac{F_1}{T_1} u_t - \frac{1}{T_1} x_2; \\ \dot{x}_3 &= x_4; & \dot{x}_4 &= \frac{F_2}{T_2} u_r - \frac{1}{T_2} x_4; \\ \dot{x}_5 &= x_6; & \dot{x}_6 &= \frac{\dot{x}_2}{l} - \frac{gx_5}{l}; \\ \dot{x}_7 &= x_8; & \dot{x}_8 &= -x_1 \frac{\dot{x}_4}{l} - \frac{gx_7}{l}; \end{aligned} \quad (15)$$

Define the sliding surface as:

$$S = [S_1 \quad S_2]^T \quad (16)$$

Where:

$$S_1 = \dot{e}_1 + \lambda_1 e_1 + \eta_1 \dot{e}_5 + \lambda_3 e_5 \quad (17)$$

$$S_2 = \dot{e}_3 + \lambda_2 e_3 + \eta_2 \dot{e}_7 + \lambda_4 e_7$$

Differentiating equation (16) with respect to time, we have:

$$\begin{cases} \dot{S} = [\dot{S}_1 \quad \dot{S}_2]^T \\ \dot{S}_1 = \ddot{e}_1 + \lambda_1 \dot{e}_1 + \eta_1 \ddot{e}_5 + \lambda_3 \dot{e}_5 \\ \dot{S}_2 = \ddot{e}_3 + \lambda_2 \dot{e}_3 + \eta_2 \ddot{e}_7 + \lambda_4 \dot{e}_7 \end{cases} \quad (18)$$

Next, we choose the constant rate reaching law for the system:

$$\begin{cases} \dot{S}_1 = -K_1 \text{sign}(S_1) \\ \dot{S}_2 = -K_2 \text{sign}(S_2) \end{cases} \quad (19)$$

Substituting equations (15)-(18) into equation (19), the control signal can be established as:

$$u_t = \frac{1}{F_1(\eta_1 + l)} [T_1 \eta_1 g x_5 + l x_2 + \eta_1 x_2 + T_1 l (\ddot{x}_{1d} - \lambda_1 (x_2 - \dot{x}_{1d}) - \lambda_3 x_6) - T_1 l K_1 \text{sgn}(S_1)] \quad (20)$$

$$u_r = \frac{1}{F_2 J (l - \eta_2 x_1)} [l x_4 - \eta_2 x_1 x_4 + T_2 \eta_2 g x_7 + T_2 l (\ddot{x}_{3d} - \lambda_2 (x_4 - \dot{x}_{3d}) - \lambda_4 x_8) - T_2 l K_2 \text{sgn}(S_2)] \quad (21)$$

To reduce the effect of the chattering phenomenon, we replace the Sign function with a saturation function as follows:

$$\text{sat}\left(\frac{s_i}{\varepsilon}\right) = \begin{cases} \text{sign}(s_i) & \text{ khi } |s_i| > \varepsilon \\ \frac{s_i}{\varepsilon} & \text{ khi } |s_i| \leq \varepsilon \end{cases}; \quad (22)$$

3.2. Stability analysis

To ensure the stability of the system, as a first step, we choose the Lyapunov function $V = \frac{1}{2} S^T S \geq 0$. Where: $\dot{V} = -K_1 |S_1| - K_2 |S_2| \leq 0$ with every $K_1 > 0$, $K_2 > 0$. This means the system can maintain sliding on the sliding surface $S = 0$. However, for each sliding surface, it is a combination of the error between the output value compared to the setpoint value and the swing angle of the cargo. Thus, this combination doesn't guarantee that all the controlled variables will converge to their references on the sliding manifold. Therefore,

we need to consider the system state on the sliding surface. Substituting $S = 0$ into equation (17), then into equation (15). Through these transformations, we obtain a space-state model represented as follows:

$$\dot{Y} = AY \quad (23)$$

where $Y = [Y_1 \ Y_2 \ Y_3 \ Y_4 \ Y_5 \ Y_6]^T$ with $Y_1 = x_5 = \alpha$; $Y_2 = x_7 = \beta$; $Y_3 = x_6 = \dot{x}_5$; $Y_4 = x_8 = \dot{x}_7$; $Y_5 = x_1 - x_{1d}$; $Y_6 = x_3 - x_{3d}$.

$$A = [A_1 \ A_2 \ A_3 \ A_4 \ A_5 \ A_6]$$

where

$$A_1 = \begin{bmatrix} 0 & 0 & \frac{\lambda_1 \lambda_3 - g}{(\eta_1 + l)} & 0 & -\lambda_3 & 0 \end{bmatrix}^T$$

$$A_2 = \begin{bmatrix} 0 & 0 & 0 & -\frac{x_1 \lambda_2 \lambda_4 + g}{l - \eta_2 x_1} & 0 & -\lambda_4 \end{bmatrix}^T$$

$$A_3 = \begin{bmatrix} 1 & 0 & \frac{\lambda_1 \eta_1 - \lambda_3}{(\eta_1 + l)} & 0 & -\eta_1 & 0 \end{bmatrix}^T$$

$$A_4 = \begin{bmatrix} 0 & 1 & 0 & -x_1 \frac{\lambda_2 \eta_2 - \lambda_4}{l - \eta_2 x_1} & 0 & -\eta_2 \end{bmatrix}^T$$

$$A_5 = \begin{bmatrix} 0 & 0 & \frac{\lambda_1^2}{(\eta_1 + l)} & 0 & -\lambda_1 & 0 \end{bmatrix}^T$$

$$A_6 = \begin{bmatrix} 0 & 0 & 0 & -x_1 \frac{\lambda_2^2}{l - \eta_2 x_1} & 0 & -\lambda_2 \end{bmatrix}^T$$

To guarantee the stability of the system, the linearized state matrix \mathbf{A} should be Hurwitz (i.e. its eigenvalues are located in the left half of the complex plane). After a series of calculations, the stability conditions are given as:

$$\begin{cases} \lambda_1 > 0 \\ \eta_1 > -l \\ \lambda_3 > \lambda_1 \eta_1 \\ \lambda_2 > 0 \\ \eta_2 x_{1d} < l \\ \lambda_4 x_{1d} < \lambda_2 \eta_2 x_{1d} \end{cases} \quad (24)$$

With the proposed HSMC controller (20)-(21), the performance quality of the tower crane not only depends on model parameters such as l , and J , but also on the parameters of the controller including λ_1 , λ_2 , λ_3 , λ_4 , η_1 , η_2 , K_1 , K_2 . In this paper, we propose the use of the PSO algorithm to find the optimal parameters for the HSMC controller, with the goal of optimizing the settling time and swing angle error of the load.

3.3. HSMC's parameter optimization

In this paper, the PSO algorithm is used to obtain 8 parameters $\lambda_1, \lambda_2, \lambda_3, \lambda_4, \eta_1, \eta_2, K_1, K_2$ of the HSMC controller base on fitness function. How this fitness function is defined depends on the optimization target of each problem. As mentioned before, the goal of this research is to reduce the settling time.

Furthermore, this paper also aims to lower the load's angle when the trolley and jig reach their reference position. From those targets, the fitness function for the PSO algorithm in this study is chosen as follows:

$$J = T_{st} + \mu E_R \quad (25)$$

where

- T_{st} is the 2% setting time of the system.
- $E_R = \sum_{t=T_{st}}^{\infty} (|\alpha(t)| + |\beta(t)|)$ is the sum of swing angles after the system has settled.
- μ : weighting factor between T and e . If $\mu > 1$, PSO will prioritize for optimizing oscillations suppression. Otherwise, with $\mu < 1$ PSO will put more effort into reducing the settling time. In this article, the value of μ is chosen as 0.1.

The PSO algorithm is population-based optimization, where "particles" represent potential solutions. Particles move in the search space and interact with each other to search for the best location. The best location will correspond to the smallest fitness function value J .

The optimization will be done by adjusting the controller's parameter. With each set of parameters, the system will have a different response. Those responses will be evaluated by the fitness function. After many iterations of adjusting parameters and evaluating the response, the optimal parameters, which have a minimum value of J , are obtained.

From the works above, the whole control system can be summarized as in Figure 2.

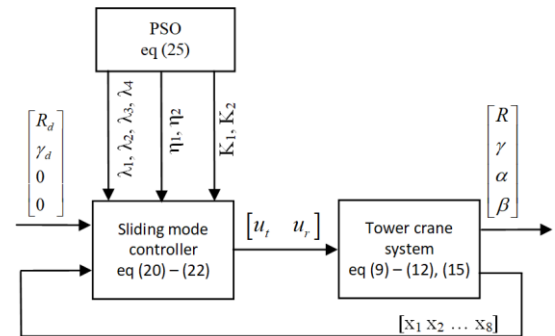


Figure 2. Tower crane control system diagram. Note that $x_1 = R, x_2 = \dot{x}_1, x_3 = \gamma, x_4 = \dot{x}_3, x_5 = \alpha, x_6 = \dot{x}_5, x_7 = \beta, x_8 = \dot{x}_7$.

4. Simulation and experimental results

4.1. Simulation and experimental setup

The parameter of the tower crane in this paper is: $T_1 = 0.01, T_2 = 0.08, F_1 = \frac{70 \times 2 \times \pi \times 0.016}{60}, F_2 = \frac{(\frac{10}{11}) \times 2\pi}{60}, l = 0.59m, g = 9.81 \frac{m}{s^2}$. The starting positions of trolley and jib are $R = 0$ m and $\gamma = 0^\circ$. The reference positions are $R = 0.3$ m, $\gamma = 45^\circ$. The boundary of controller parameters is detailed in (24). Control signal boundary is $\pm 10V$ for u_t and $\pm 10V$ for u_r .

In the next stage, PSO is started in Matlab/Simulink. First, a population of 50 particles is initialized. The maximum iteration is $K_{max} = 100$. With the PSO algorithm, the optimal parameter is obtained after K_{max} iterations.

This study is deployed on a tower crane model in the WSR laboratory of Hanoi University of Science and Technology. The tower crane model's structure is specified in Figures 3

and 4. The tower crane model has 2 moving axes driven by 2 servo transmission systems. Axis 1 is the rotation of the jib controlled by a servo motor accompanied by a high-ratio reduction gearbox. The transmission number is 1:11. The other axis is the forward motion of the trolley along the jib. The trolley is driven by a similar servo motor. Both motors used in the experiment are now in speed control mode. The entire system is controlled by the NI myRIO 1900 microcontroller, Table 1 describes the parameters of the servo motor. Labview software is used to program, control, and monitor the system. After obtaining the full parameters of the model and controller, the research was implemented on system simulation on Matlab/Simulink and then on the experimental model. Two scenarios are implemented in simulation and experiment to compare and evaluate the effectiveness of the parameter set that is determined by PSO:

- **Scenario 1:** The parameter of the SMC controller is selected manually.
- **Scenario 2:** Using the SMC controller parameters specified by the PSO algorithm.

Parameter sets of two scenarios are described in Table 2.

Table 1: Motor parameters

	Trolley's motor	Jib's motor
Rated output	200 W	200 W
Rated torque	1.27 N.m	1.27 N.m
Rated Speed	3000 rpm	3000 rpm
Inertia torque	$0.018 * 10^{-4} \text{ kg.m}^2$	$0.018 * 10^{-4} \text{ kg.m}^2$
Speed coefficient	$70 \frac{\text{rpm}}{\text{V}}$	$10 \frac{\text{rpm}}{\text{V}}$

Table 2: Controller parameters

SMC	SMC-PSO
$\lambda_1 = 1 \quad \lambda_2 = 0.9$	$\lambda_1 = 1.01 \quad \lambda_2 = 0.98$
$\lambda_3 = 1.1 \quad \lambda_4 = -1.5$	$\lambda_3 = 2.196 \quad \lambda_4 = -2.07$
$\eta_1 = 0.05$	$\eta_1 = 0.05$
$\eta_2 = -0.01$	$\eta_2 = -0.012$
$K_1 = 25 \quad K_2 = 70$	$K_1 = 35 \quad K_2 = 75$

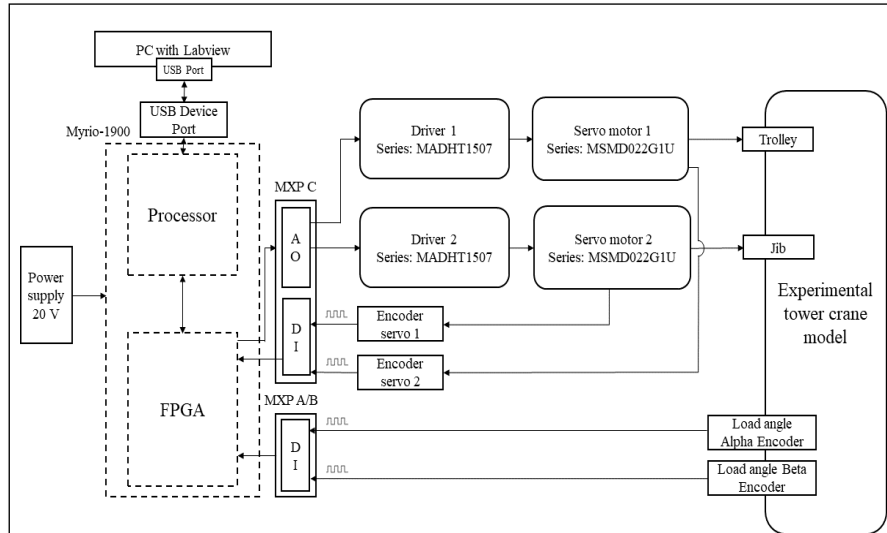


Figure 3. Experimental diagram.

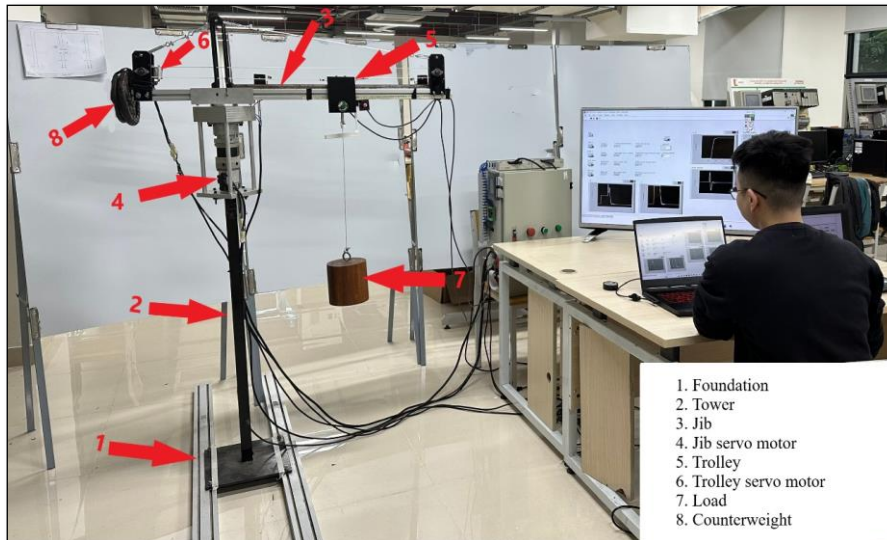


Figure 4. Experimental setup.

4.2. Simulation results

The results of the load angles α and β in Figure 5 show that with the use of the PSO-SMC controller, the settling time of the angles α and β are 2.5 seconds and 6.5 seconds, respectively. Meanwhile, when using the SMC controller without optimal parameters, the settling time of angles α and β is 7 seconds and 8.5 seconds. From these results, we can see the anti-vibration effectiveness of the PSO-SMC controller. Figure 6 is the result of the position response R of the trolley and the rotation angle γ of the jib. The results show that when

applying the PSO-SMC controller, the response time of rotation angle γ decreases from 4.2 seconds to 3.51 seconds. This result shows that the PSO algorithm has reduced the system setup time, as set out in section 4.1.

The voltage signals controlling the trolley u_t and the jib u_r are depicted in Figure 7, we can see that the PSO-SMC controller helps reduce the fluctuation of the control signal. This is achieved thanks to the rapid anti-vibration effect that the proposed controller provides.

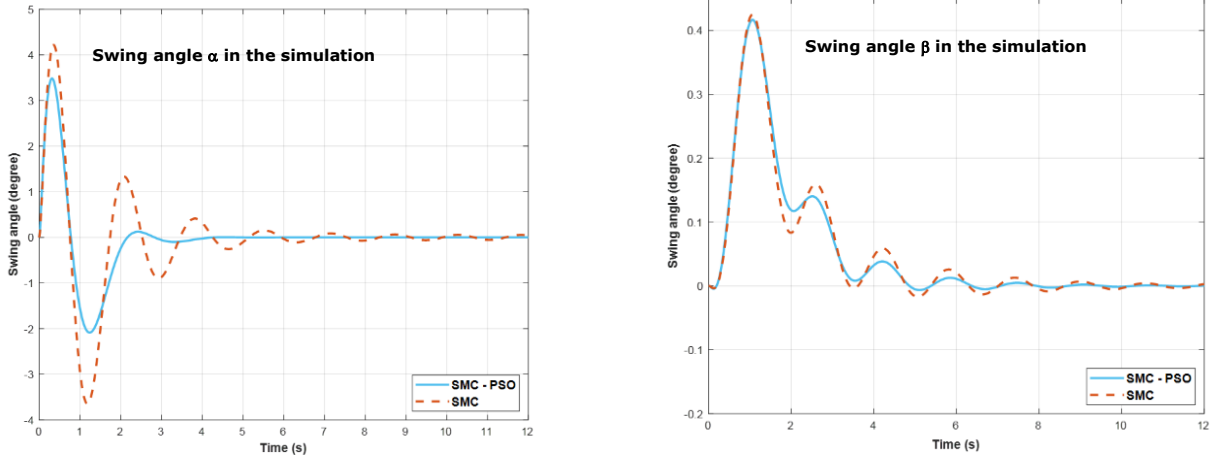


Figure 5. Load swing angle α and β in simulation.

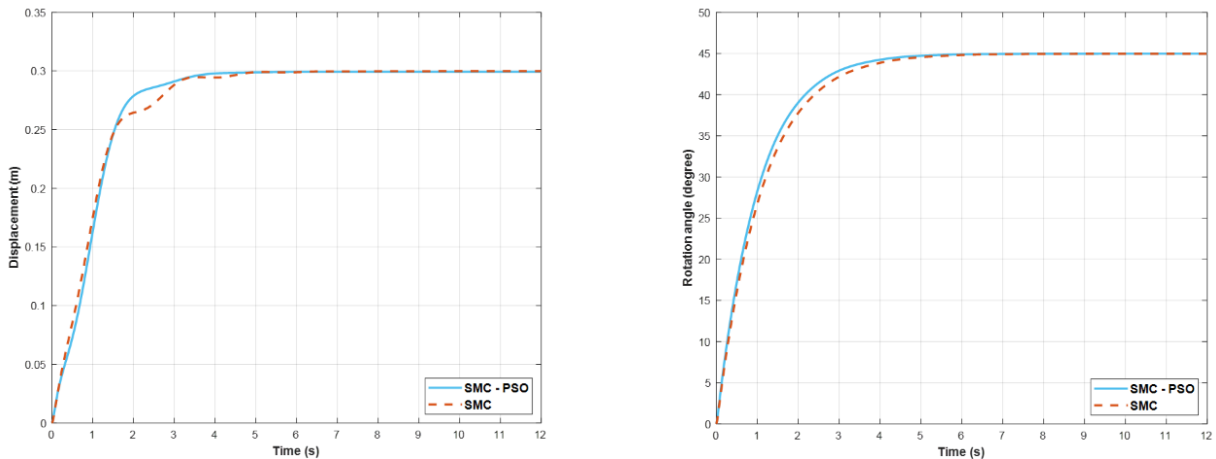


Figure 6. Trolley position in the jib and jib rotation angle in simulation.

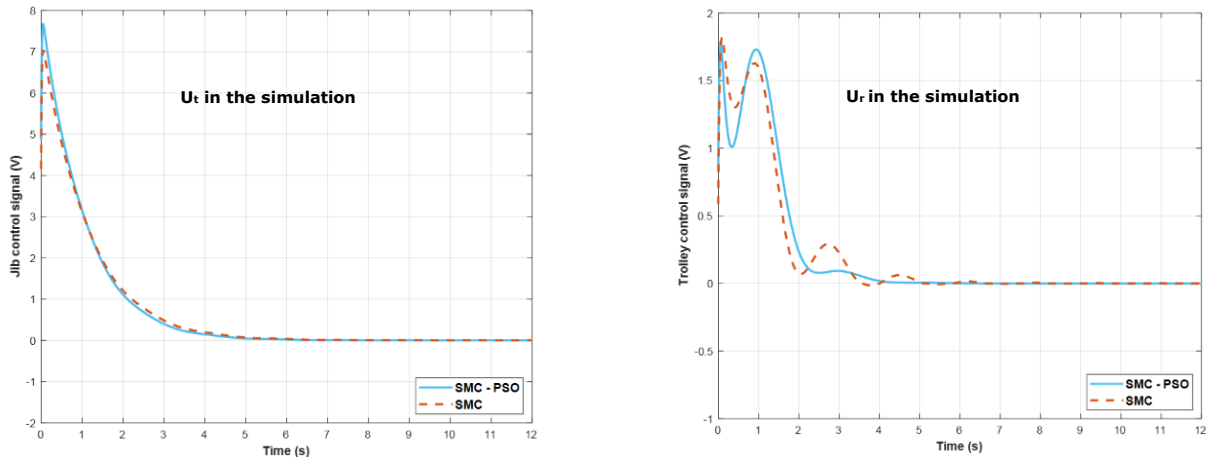


Figure 7. The control signal U_r and U_t in simulation

4.3. Experimental result

Experimental results Figure 8 verifies the anti-vibration effectiveness as mentioned in the simulation results above. When combining PSO with SMC, the oscillation angles α and β of the load are extinguished at the 5th second. Meanwhile, in the SMC controller with randomly selected parameters in scenario 1, the oscillation time of angles α and β is up to 11 seconds. Through this, we conclude that the PSO-SMC controller brings efficient oscillation suppression.

Figure 9 is the response of the trolley and jib when deployed on the experimental model. The jib settling time changes from 7.36 seconds to 6.27 seconds when applying the parameter set specified by PSO.

Figure 10 is the experimental result of the voltage signal controlling the trolley u_t and the jib u_r . Similar to the simulation results in Figure 6, when the oscillation phenomenon of the control signals u_r and u_t of the PSO-SMC controller is minimized.

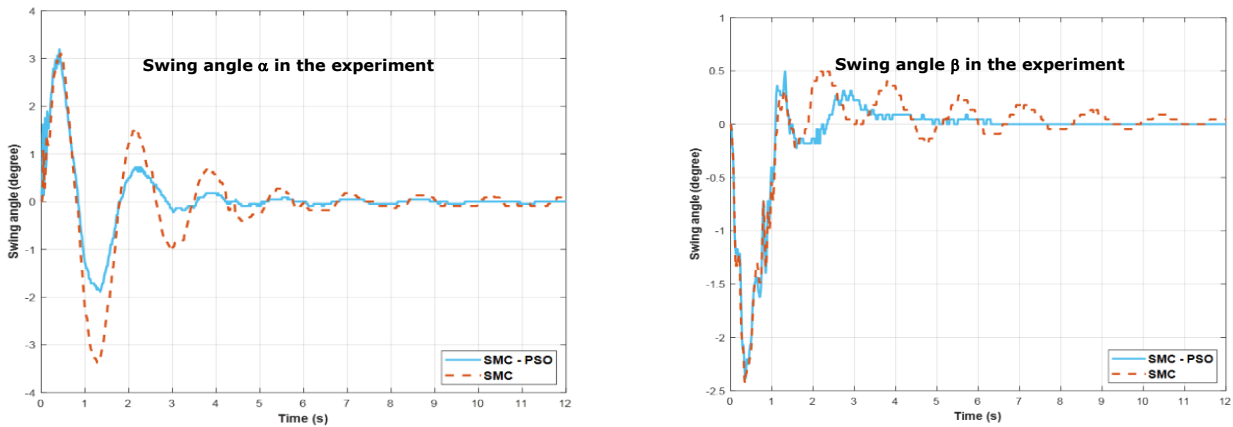


Figure 8. Load swing angle α and β in the experiment.

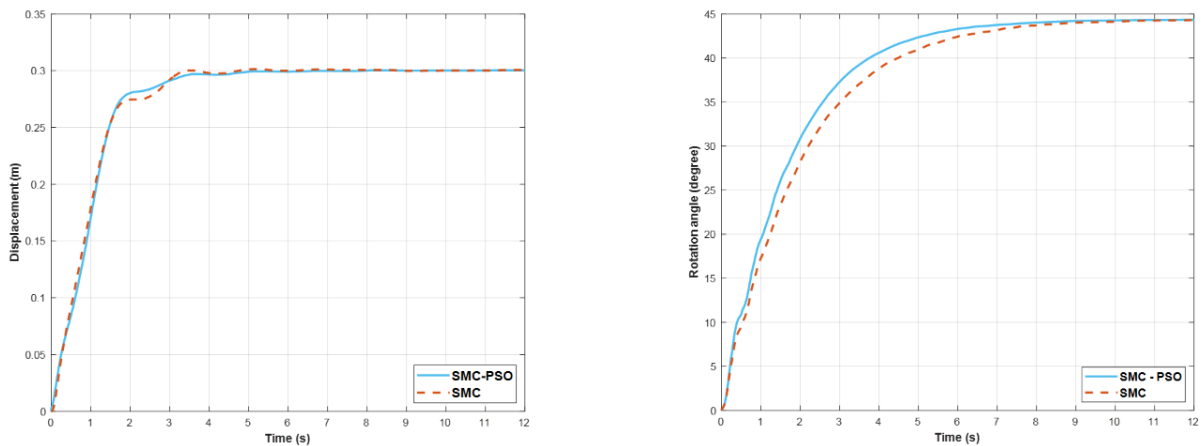


Figure 9. Trolley position in the jib and jib rotation angle in the experiment.

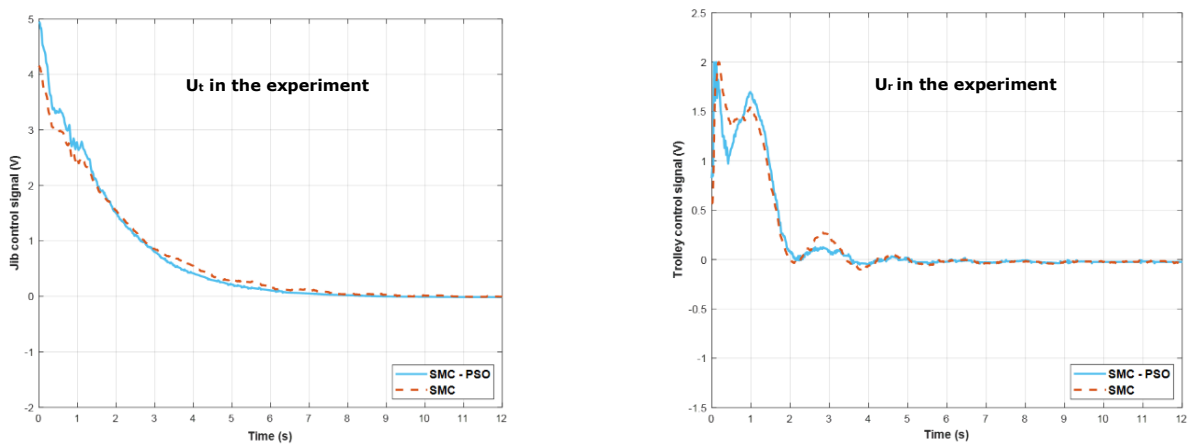


Figure 10. The control signal U_r and U_t in the experiment.

4.4. Evaluation of simulation and experimental results

From the results of simulation and experiment, we have a table of optimal results as shown in Table 3.

Table 3: Results comparison table.

		SMC	SMC-PSO
Simulation	System settling time	4.2s	3.51s
	Fitness function value J	4.34	3.53
Experiment	System settling time	7.36s	6.27s
	Fitness function value J	12.98	7.58

From Table 3, when using only the independent SMC controller, the settling time of the simulation system is 4.2 seconds, and the objective function value is 4.34. However, after integrating the PSO algorithm, this settling time is reduced to 3.51 seconds, and the objective function value is 3.53. In the experimental results, when using the PSO-SMC controller, the system settling time is only 6.27 seconds compared to 7.36 seconds when using the SMC controller. In addition, the objective function value is also reduced by 1.76 times.

Although there is a difference between the experimental and simulation results, both results show that the PSO-SMC controller provides higher anti-swinging performance and shorter settling time. This difference can be explained by the discrepancy between the real system and its mathematical model.

5. Conclusion

This article has presented an anti-vibration control method for tower cranes using the SMC sliding controller combined with the PSO optimization algorithm. Simulations and experiments have been implemented to demonstrate the correctness of this control method. After comparing the simulation and experimental results of the proposed controller with the SMC controller, some assessments are drawn including the PSO-SMC controller has a faster settling time (respectively 8.32% for simulation and 41.22% for experiment), along with the ability to suppress load vibrations faster as shown in Figure 4 and Figure 8. From these results, the combination between the PSO algorithm and SMC controller helps reduce system settling time, while improving anti-vibration efficiency. However, the disadvantage of the SMC controller is that the system's control signals change too quickly. This phenomenon is called "Chattering", which can cause high-frequency oscillations that adversely affect the system. Although after integrating the PSO algorithm, this phenomenon has been reduced thanks to the ability to quickly reduce vibration, the problem has not been completely resolved. Therefore, in the future, we will consider combining the PSO-SMC controller with the input signal shaping method. Finally, the above control method will also be considered and researched for implementation in tower crane systems with variable rope lengths.

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